

TECHNICAL MEMORANDUM: THRIE-BEAM RETROFIT PHASE 2 -APPLICATION OF A NEW DESIGN WITHOUT A CURB FOR *MASH* TL-3 AND PERFORMANCE AND IMPROVEMENTS FOR *MASH* TL-4 (TTI PROJECT 619601)



Sponsored by the



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	SI* (MODE	RN METRIC) CONVER	SION FACTORS	
	APPROXI	MATE CONVERSIONS	S TO SI UNITS	
Symbol	When You Know	Multiply By	To Find	Symbol
		LENGTH		
in	inches	25.4	millimeters	mm
ft	feet	0.305	meters	m
yd	yards	0.914	meters	m
mi	miles	1.61	kilometers	km
		AREA		
in ²	square inches	645.2	square millimeters	mm ²
ft ²	square feet	0.093	square meters	m ²
vd ²	square vards	0.836	square meters	m ²
ac	acres	0 405	hectares	ha
mi ²	square miles	2 59	square kilometers	km ²
	square miles	VOLUME	square mometers	
floz	fluid ounces	29 57	milliliters	ml
gal	gallons	3 785	liters	1
ft ³	cubic feet	0.028	cubic meters	m ³
vd ³	cubic vards	0.020	cubic meters	m ³
yu	NOTE: volumes	greater than 1000Ls	hall be shown in m^3	
	NOTE. Volumes			
07	0110505	20.25	grappe	a
02	buildes	20.55	gians	g ka
	pounds	0.454	Kilograffis	Kg
1	snort tons (2000 lb)	0.907	megagrams (or metric ton")	Nig (or "t")
05		APERATURE (exact d	egrees)	26
۳F	Fahrenheit	5(F-32)/9	Celsius	°C
		or (F-32)/1.8		
	FOR	CE and PRESSURE or	r STRESS	
lbf	poundforce	4.45	newtons	N
lbf/in ²	poundforce per square inch	6.89	kilopascals	kPa
	APPROXIM	IATE CONVERSIONS I	FROM SI UNITS	
Symbol	When You Know	Multiply By	To Find	Symbol
		LENGTH		
mm	millimeters	0.039	inches	in
m	meters	3.28	feet	ft
m	meters	1.09	yards	yd
km	kilometers	0.621	miles	mi
		AREA		
mm ²	square millimeters	0.0016	square inches	in ²
m ²	square meters	10.764	square feet	ft ²
m ²	square meters	1.195	square yards	yd ²
ha	hectares	2.47	acres	ac
km ²	Square kilometers	0.386	square miles	mi ²
		VOLUME		
ml	milliliters	0.034	fluid ounces	07
1	liters	0 264	gallons	gal
m ³	cubic meters	35 314	cubic feet	ft ³
m ³	cubic meters	1 307	cubic vards	vd ³
	cubic meters	MASS		yu
~	arama.	0.025	0110505	07
g	grans	0.035	ounces	02 Ib
Kg		2.202	pourius	ui T
ivig (or "t")	megagrams (or "metric ton")	1.103	snort tons (2000b)	I
	TEN	A DE CARTORE (EXACT D	egrees)	0 F
°C	Celsius	1.8C+32	Fahrenheit	۳F
	FOR	ICE and PRESSURE or	STRESS	
N	newtons	0.225	poundforce	lbf

*SI is the symbol for the International System of Units

CHAPTER 1. INTRODUCTION & BACKGROUND

1.1. PROBLEM STATEMENT AND BACKGROUND

Many bridge rails in the United States are outdated with respect to the Manual for Assessing Safety Hardware (*MASH*^[1]). It is not economically feasible to completely replace the obsolete bridge rails with newer *MASH*-compliant designs. Oftentimes, state transportation agencies may need to utilize a crash-worthy bridge rail that is retrofit to the existing bridge deck when an obsolete bridge railing needs to be replaced for a *MASH*-compliant bridge rail system.

In the preceding research (referred to as 'Phase 1' herein), TTI has designed and successfully crash-tested a new Thrie-beam retrofit bridge rail design to be used on obsolete bridges ^[2]. Details of Phase 1 crash-tested design are shown in Figure 1.1.



Figure 1.1. Details of Thrie-beam Bridge Rail Retrofit^[2]

Actual conditions on bridges may vary from this as-tested design. Several conditions such as no curb, taller curb, wider curb, changes in deck thickness and reinforcing steel, and the location of existing obsolete bridge rails left in place will differ from the as-tested design. Thus, following questions arose to apply this Thriebeam bridge rail retrofit for more bridge conditions:

- Can the as-tested design be used for bridge rails without a curb at TL-3?
- How does the as-tested design perform for *MASH* TL-4?
- What changes are needed to the as-tested design to meet MASH TL-4?

In the present project (Phase 2), TTI researchers conducted a study to answer these questions using LS-DYNA simulations.

1.2. OBJECTIVE

The main objective of this project will be to perform LS-DYNA simulations on the as-tested design using no curb for *MASH* TL-3. If necessary, modification(s) will be made to the design to improve performance to meet *MASH* TL-3 specifications. In addition, LS-DYNA simulations will be performed on the as-tested design for *MASH* Test 4-12. If necessary, modification(s) will be made to the design to improve performance for *MASH* Test 4-12.

1.3. BENEFITS

The main benefit of this project will be to expand the use of a new Thriebeam retrofit system to bridge rails without a curb to meet the crash requirements of *MASH* TL-3. Also, this project will investigate if a new Thrie-beam retrofit system can be used for *MASH* TL-4 and explore what changes are needed (if any) to the astested design to improve performance for satisfying *MASH* TL-4. This will provide broader retrofit options using a new Thrie-beam for more existing bridge rails.

1.4. **PRODUCTS**

Brief letter report summarizing the simulation efforts, design, and details for both the no curb *MASH* TL-3 design and the *MASH* TL-4 design (2 designs). Professional opinions (separate tasks outside the scope and funding for this project, for each) can be provided for the following conditions:

- Taller curb (approx. 9 inches)
- Wider curb (approximately 24 inches)

- Substandard bridge deck conditions (thinner deck, less reinforcing, lower compressive strength (1 case here for further review after the results are reviewed from this project).
- Existing obsolete bridge rails that are left in place, i.e., reviewing the working width from the TL-3 crash test to determine if existing rails left in place will influence performance.

1.5. WORK PLAN

For this project, TTI investigates whether the as-tested Thrie-beam retrofit design bridge rail without a curb meets *MASH* TL-3 requirements. The as tested Thrie-beam retrofit design will be modified accordingly to meet the *MASH* specifications if necessary. Also, the application of the as-tested Thrie-beam for *MASH* TL-4 specification will be explored. TTI plans to develop engineering drawings of the proposed details using SolidWorks. The crashworthiness of proposed designs will be evaluated using LS-DYNA simulation to examine that required *MASH* test level requirements are met for each design. This project focuses on developing engineering design details and evaluating crashworthiness using computer simulation; no testing is planned for this project. The work plan is as follows:

- 1.) Task 1: Engineering Analyses & Detailing of Retrofit Designs for MASH TL-4 -TTI will develop details of the new Thrie-beam retrofit system without a curb. Particularly, TTI proposes connection details between existing deck and Thriebeam bridge rail retrofit. The proposed design will be analyzed as per the strength analysis of the current AASHTO LRFD, Section 13 Design Specifications ^[3] and modified accordingly to meet MASH TL-3 requirements. The strength analysis using MASH TL-4 loading conditions will be also performed on the as-tested design, and modifications will be proposed if necessary for MASH TL-4.
- 2.) Task 2: TTI will prepare engineering drawings of the proposed details for both designs from Task 1 using SolidWorks.
- 3.) Task 3 Simulations of As-Tested Design without a Curb for *MASH* TL-3 TTI will perform crashworthiness evaluation on the as-tested Thrie-beam bridge rail retrofit with no curb at *MASH* TL-3. TTI will generate simulation models using LS-DYNA and assess evaluation criteria including structural adequacy and occupant risk. Design modification will be proposed if necessary.

- 4.) Task 4 Simulations of AS-Tested Design with a Curb for *MASH* TL-4 Same as Task 3, TTI will perform crashworthiness evaluation on the as-tested Thriebeam bridge rail retrofit at *MASH* TL-4. TTI will generate simulation models using LS-DYNA and assess evaluation criteria including structural adequacy and occupant risk. Design modification will be proposed if necessary.
- 5.) Task 5 Brief Letter Report Summarizing the from Tasks 1 to 4 TTI will prepare a brief letter report summarizing the results from Task 1 1 to 4.

CHAPTER 2. FINITE ELEMENT MODEL DEVELOPMENT

For this project LS-DYNA computer simulations were performed to determine the predictive behavior of the designs evaluated for this study. The FE models developed for this project were developed using the same conditions as a full-scale crash testing to compare the results. Representative vehicle models for the small car (*MASH* Tests 3-10 and 4-10) and the pickup truck (*MASH* Test 3-11 and 4-11), and single unit truck (*MASH* Test 4-12) were used for this project. A discussion of the simulations performed on the various systems investigated for this project are discussed as follows in Chapter 3.

3D finite element models of two bridge rail systems were developed. LS-PrePost was used as the primary tool to develop the models. The first model represented the full-scale system that was tested and evaluated with full-scale crash testing (2). Another variation of the crash tested system was developed that did not include a curb. Figure 2.1 through Figure 2.4 shows the finite element model of the Thrie-beam Retrofit system. Figure 2.5 and Figure 2.6 shows the finite element model of the Thrie-beam Retrofit system without a curb.







Figure 2.2. Overall View of Thrie-beam Retrofit Finite Element Model.



Figure 2.3. Side View of Thrie-beam Retrofit Finite Element Model.

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Figure 2.4. Top View of Thrie-beam Retrofit Finite Element Model.



Figure 2.5. End View of Thrie-beam Retrofit (without Curb) Finite Element Model.



Figure 2.6. Overall View of Thrie-beam Retrofit (without Curb) Finite Element Model.

The concrete deck and curb were modeled with Solid elements and MAT_CSCM_Concrete. A concrete strength of 3300 psi was used in the model. A damage-based failure criterion was incorporated into the material model to allow

for the prediction of concrete damage. The reinforcement was modeled with Beam elements and MAT_PIECEWISE_LINEAR_PLASTICITY. A 40 ksi yield strength was used for the reinforcement. The steel posts and Thrie-beam rail were modeled with shell elements and MAT_PIECEWISE_LINEAR_PLASTICITY. The wood blockouts were modeled with solid elements and MAT_ELASTIC. A boundary condition was applied on the end of the deck to simulate attachment to a bridge deck superstructure.

CHAPTER 3. COMPUTER SIMULATIONS

Finite element analysis of the models was performed using impact computer simulations. The simulations were conducted using LS-DYNA, a commercial general purpose nonlinear finite element analysis code capable of simulating complex engineering systems with impact-contact phenomena.

Two systems were evaluated with finite element computer simulations. First, the Thrie-beam Retrofit finite element was evaluated according to *MASH* TL-4. This consisted of conducting a *MASH* Test 4-12 impact with the computer simulations. Second, the Thrie-beam Retrofit without a curb finite element model was evaluated according to *MASH* TL-3. The finite element computer simulation evaluation of the systems is presented in the below sections.

3.1. FINITE ELEMENT MODEL VALIDATION

To validate the behavior of the finite element developed and discussed in Chapter 2, computer simulations were performed replicating the previous full-scale crash test *MASH* Test 3-11 impact conditions (*2*). The impact speed was 62.0 mi/h and the impact angle was 25.1 degrees. The impact location was 8.2 ft upstream of the centerline of post 16.

Figure 3.1 and Figure 3.2 show a comparison of the computer simulation and full-scale crash impact. The computer simulation indicated similar performance to the full-scale crash test. The computer simulation vehicle was redirected and showed similar vehicle kinematics to the full-scale crash test. The occupant risk factors were comparable (Table 3.1) between the computer simulation and full-scale crash test.

Overall, the finite element indicated similar behavior and characteristics when compared to the full-scale crash test. Thus, this finite element model was used in the predictive computer simulations presented in the later sections in this chapter.















0.3 sec



0.0 sec



0.1 sec







0.3 sec

Figure 3.1. Comparison of FE Computer Simulation and Full-Scale Crash Test (Gut View).



0.0 sec



0.0 sec



0.1 sec



0.1 sec



0.2 sec













Test Parameter	Crash Test	Computer Simulation
OIV, Longitudinal (ft/s)	26.3	18.7
OIV, Lateral (ft/s)	25.3	28.6
Ridedown, Longitudinal (g)	8.2	3.4
Ridedown, Lateral (g)	7.6	14.7
Roll (deg.)	20.0	22.1
Pitch (deg.)	9.0	4.1
Yaw (deg.)	41.0	37.5

Table 3.1. Comparison of Occupant Risk Factors for Full-Scale Crash Test andFE Computer Simulation.

3.2. THRIE-BEAM RETROFIT - MASH TL-4 EVALUATION

To evaluate the performance of the Thrie-beam Retrofit bridge rail system under *MASH* TL-4 conditions, a series of computer simulations for *MASH* Test 4-12 with the SUT vehicle model was performed. This system was previously evaluated with full-scale crash testing according to *MASH* Test 3-11 (*2*). Thus, there was no need to perform computer simulations with the small car (*MASH* Test 4-10) or pickup truck (*MASH* Test 4-11) vehicle impacts.

The SUT vehicle impacted the bridge rail at an impact speed and angle of 56 mi/h and 15 degrees. The impact point was 5 ft upstream of middle of the bridge deck where the concrete joint exists. This impact point maximized the damage on bridge deck and was considered the critical impact point for testing.

Based on the results of the simulations, several design changes were made to improve the performance of the bridge rail system. These changes were then also modeled and new impact simulations were performed to arrive at the final retrofit design to make a recommendation for full-scale crash testing.

3.2.1. As-Tested Design with a Curb

First, the researchers performed *MASH* Test 4-12 simulation on the *MASH* TL-3 compliant bridge railing system which was tested in the previous project [2].

Based on the computer simulation, the bridge rail deflection was minor: the maximum dynamic and permanent deflection of the guardrail system was 4 inches and 3.26 inches, respectively. However, the box of SUT excessively leaned over the rail with the maximum intrusion width of 10.73 ft. When the front bottom corner of

the box was torn and tended to go over the rail, the cab also engaged with the rail and tended to go over the rail. Figure 3.3 shows the vehicle behavior at impact and maximum box lean. Since the as-tested system could not contain the vehicle and could not meet *MASH* TL-4 evaluation criteria, the researchers decided to increase the rail height to improve the vehicle stability during impact.



Figure 3.3. Test 4-12 Simulation Images for 34-inch Tall Thrie-beam System.

3.2.2. Different Heights

To investigate the performance of the Thrie-beam rail with a taller rail height, the height of the Thrie-beam rail was increased to 38 inches. The 38-inch tall system was evaluated with the same impact conditions.

Figure 3.4 shows the simulation images showing when impacting the rail and when the maximum intrusion was observed. Similar to the as-tested system, when the front bottom corner of the box hit the rail, the box overrode the rail, and the system likely failed to contain the vehicle. The maximum intrusion width was 10.7 ft, which was not different from that for the as-tested system. The 38-inch tall system did not indicate satisfactory performance in redirecting and containing the SUT vehicle. Thus, the researchers increased the rail height by an additional 4 inches to improve vehicle stability.



Figure 3.4. Test 4-12 Simulation Images for 38-inch Tall Thrie-beam System.

As shown in Figure 3.5, the SUT vehicle was successfully contained and redirected in the simulation with the 42-inch tall system. The maximum dynamic and permanent deflection of the guardrail system was 5.3 inches and 3.8 inches, respectively. The maximum intrusion width was 9.5 ft, which is 1.2 ft (approximately 15 inches) less than that for both the as-tested system and the 34-high system. Based on the simulation results, the Thrie-beam system with a 42-inch height could be expected to pass *MASH* Test 4-12 evaluation criteria in a full-scale crash test.



Figure 3.5. Test 4-12 Simulation Images for 42-inch Tall Thrie-beam System.

As the height of the barrier increases, there is less vehicle roll and more floor box is engaged in the impact, thereby increasing the impact load (shown in Figure 3.4). At a 36-inch and 38-inch rail height, the box overrides and over-engaged to the rail, while the box floor contact the rail in early stage and contained and redirected vehicle at 42-inch high rail.



After evaluating the performance of the Thrie-beam retrofit system according to *MASH* Test 4-12, it was necessary to evaluate the performance according to *MASH* Test 4-11 to determine the effect of the increased rail height.

A *MASH* Test 4-11 computer simulation was performed with pickup truck vehicle model impacting the 42-inch tall Thrie-beam system. Due to the large opening between the Thrie-beam and curb, the impact side front tire was snagged, and the vehicle could not be redirected as shown in Figure 3.7. Thus, it was recommended to modify the system to improve the performance for the *MASH* Test 4-11 impact conditions.



Figure 3.7. *MASH* Test 4-11 Computer Simulation with 42-inch Tall Thrie-beam System.

3.2.3. 42-inch Tall Thire Beam Retrofit System with Rubrail

While the 42-inch tall Thrie-beam retrofit system performed adequately for *MASH* Test 4-12, the performance was unsatisfactory for *MASH* Test 4-11 due to the large opening between the curb and the bottom of the rail. This large opening allowed severe wheel snag and high vehicle accelerations. Therefore, the researchers decided to retrofit the 42-inch tall Thrie-beam system.

The first modification option was to add a rubrail to the 42-inch Thrie-beam system. *MASH* Test 4-11 was performed for the 42-inch Thrie-beam system with a rubrail. Figure 3.8 shows the sequential images for the simulation performed on the 42-inch Thrie-beam system with a rubrail.



(c) Vehicle parallel to the system (d) vehicle exiting the system **Figure 3.8. Test 4-11 Simulation on 42-inch Thrie-beam System with Rubrail.**

The vehicle was successfully contained and redirected without tire snagging. However, no *MASH* compliant transition system can be used to connect the Thriebeam system higher than 36 inches to a *MASH* compliant W-beam system and terminal. Therefore, the research team and technical representatives decided to add a hollow structural section (HSS) tube to the top of the as-tested Thrie-beam rail system. This would allow the top of the Thrie-beam rail to stay at 34 inches. This modified system was evaluated as discussed in the next section.

3.2.4. 42-inch Tall Thire Beam Retrofit System with Top HSS Tube

A previous research study was performed that developed a *MASH* TL-4 compliant guardrail system. The system included a HSS tube attached to the top of

a standard W-beam guardrail system to increase the rail height. The system successfully met the *MASH* TL-4 evaluation criteria [3]. A transition system for the upper tube was also successfully tested and evaluated for *MASH*. This *MASH* TL-4 design concept will be referred as TxDOT *MASH* TL-4 guardrail system herein.

To increase the height of the Thrie-beam retrofit system and maintain the 34inch Thrie-beam rail height, a design concept of TxDOT *MASH* TL-4 guardrail system was adapted. An HSS (10-inch x 4-inch x ¼-inch) rail was added to the top of the astested Thrie-beam system (34 inches tall). This resulted in an increased overall system height of 43 inches. Figure 3.9 shows a detailed drawing layout of the modified system. This modified design keeps Thrie-beam at 34 inches high from the deck and enables use of the existing *MASH* compliant transition system to connect a Thrie-beam rail to a standard W-beam guardrail and terminal system.



Figure 3.9. *MASH* TL-4 Thrie-beam Bridge Rail Design Retrofitted by HSS Tube.

To evaluate the crashworthiness of the retrofitted system, a finite element model was developed, and a *MASH* Test 4-12 simulation was performed on the retrofitted system.

The HSS tubular rail and HSS rail attachment brackets were represented with elastic-plastic material models. The HSS beam in the model was unrestrained at each end of the model because the HSS rail tube primarily works by providing lateral bending stiffness to the system and does not require anchoring at the ends. Figure 3.10 presents images of the overall guardrail system model, as well as closer details of the various key components of the model.



(a) Overall System



Figure 3.10. MASH TL-4 Thrie-beam Retrofitted Design.

MASH Test 4-12 impact simulation with the SUT model was performed on the developed FE model. The vehicle impacted the bridge rail at an impact speed and angle of 56 mi/h and 15 degrees. The previously determined impact point of 5 ft upstream of a post was used.

Results of the simulation are presented in Figure 3.11. The SUT vehicle was successfully contained and redirected in the simulation. The maximum dynamic

deflection of the guardrail system was 17.7 inches. The permanent deflection was 15.3 inches. Results of the simulation showed that the modified Thrie-beam retrofit design should be considered satisfactory for *MASH* Test 4-12 evaluation criteria.



Figure 3.11. FE Simulation Sequential Images for Retrofitted Thrie-beam System.

The impact simulations for *MASH* Tests 4-10 and 11 with the small car and the pickup truck model were not performed. Since the Thrie-beam system with a 34-inch tall rail height has already met *MASH* TL-3 evaluation criteria (*2*), the retrofitted system is expected to provide satisfactory performance when the small car and the pickup truck impact the system.

Based on the impact simulation results presented herein, the research team recommends performing full-scale *MASH* TL-4 testing with the retrofitted Thriebeam system as a next step.

3.3. THRIE-BEAM RETROFIT WITHOUT CURB - MASH TL-3 EVALUATION

To evaluate the performance of the Thrie-beam Retrofit bridge rail system without a curb under *MASH* TL-3 conditions, a series of computer simulations for *MASH* Test 3-10 with the small car model and *MASH* Test 3-11 with the pickup truck model were performed. The vehicles impacted the bridge rail at an impact speed and angle of 62 mi/h and 25 degrees. The impact point was 3.6 ft upstream of the concrete joint for the Test 3-10 computer simulation. The impact point was 4.3 ft upstream of the concrete joint for the Test 3-11 computer simulation.

Figure 3.10 present sequential images from the Test 3-10 simulation impact event. The bridge rail system successfully contained and redirected the small car vehicle. The vehicle remained stable throughout the impact event. Table 3.1 shows the occupant risk parameters. The occupant risk values were within the *MASH* limits. The Thrie-beam Retrofit system without a curb indicated satisfactory performance for *MASH* Test 3-10.

Figure 3.11 present sequential images from the Test 3-11 simulation impact event. The bridge rail system successfully contained and redirected the pickup truck vehicle. The vehicle remained stable throughout the impact event. Table 3.2 shows the occupant risk parameters. The occupant risk values were within the *MASH* limits. The Thrie-beam Retrofit system without a curb indicated satisfactory performance for *MASH* Test 3-11.

Based on the results of the simulations, the small car and the pickup truck performed acceptably with respect to the *MASH* criteria for *MASH* Tests 3-10 and 3-11. Thus, the Thrie-beam Retrofit system without a curb should be considered acceptable as a *MASH* TL-3 compliant bridge rail system.



Figure 3.12. FE Simulation Sequential Images for Thrie-beam System without Curb – *MASH* Test 3-10.



Figure 3.13. FE Simulation Sequential Images for Thrie-beam System without Curb – *MASH* Test 3-11.

Test Parameter	MASH Limit	Measured
OIV, Longitudinal (ft/s)	≤40.0	23.1
OIV, Lateral (ft/s)	≤40.0	30.0
Ridedown, Longitudinal (g)	≤20.49	3.6
Ridedown, Lateral (g)	≤20.49	10.0
Roll (deg.)	≤75	6.5
Pitch (deg.)	≤75	4.0
Yaw (deg.)	N/A	36.8

Table 3.2. Occupant Risk Results for *MASH* Test 3-10 Simulation.

Table 3.3. Occupant Risk Results for *MASH* Test 3-11 Simulation.

Test Parameter	MASH Limit	Measured
OIV, Longitudinal (ft/s)	≤40.0	17.9
OIV, Lateral (ft/s)	≤40.0	27.4
Ridedown, Longitudinal (g)	≤20.49	3.4
Ridedown, Lateral (g)	≤20.49	13.7
Roll (deg.)	≤75	12.8
Pitch (deg.)	≤75	3.0
Yaw (deg.)	N/A	40.7

CHAPTER 4. STRUCTURAL ANALYSIS

An engineering strength analysis was performed on the new *MASH* TL-4 design as shown in Figure 3.9 in Chapter 3. The strength analysis was performed in accordance with the American Association of State Highways and Transportation Officials (AASHTO) Load and Resistance Factor Design, Section 13 Specifications (4). The calculated strength of the 43 inches high bridge rail was 113 kips @ 30 inches height. Based on this calculated strength, the design shown in Figure 3.9 satisfies the strength requirements for *MASH* TL-4 with post spacing a at 3'-1 ½" inches on centers. For additional information, please refer to the calculations shown in Appendix A.

CHAPTER 5. SUMMARY & CONCLUSIONS

- 1.) Task 1: Engineering Analyses & Detailing of a new retrofit designs for *MASH* TL-4 was developed for this project. This new design utilized a HSS 10x4x3/8 tube mounted to the top of the Thrie-beam Retrofit Design previously tested to *MASH* TL-3 using post spacing of 3'-1 1 /2" on centers. The total height of this design was 43 inches. LS-DYNA simulations using the *MASH* TL-4 Vehicle (SUT) were successful. Engineering strength analyses were performed on the new retrofit design. The calculated strength was 100 kips at 30 inches height. This new design meets the strength requirements of *MASH* TL-4 (80 kips at 30 inches height). The new design shown herein is recommended for *MASH* TL-4 applications.
- 2.) Task 2: TTI has prepared engineering details of this recommended design retrofit. These details are shown in Figure 3.9 and in the calculations in Appendix A. This design is recommended for *MASH* TL-4.
- 3.) Task 3 Simulations of As-Tested Design without a Curb for *MASH* TL-3 were performed. The As-Tested design without a curb is recommended for *MASH* TL-3. No design modifications were needed for *MASH*-TL-3.
- 4.) Task 4 Simulations were performed on the as-tested Design with a Curb for *MASH* TL-4. Due to strength and instability of the SUT, this design (As-Tested for *MASH* TL-3 under TTI Project 615131) is not recommended for *MASH* TL-4.

REFERENCES

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APPENDIX A. CALCULATIONS



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(1) General Information and Inputs:

1) Reference: AASHTO MASH Condictions 2) Assess the adequacy of the barrier based on AASHTO LRFD Section 13 criteria

(1a) General Inputs:

f' = 4.000 hoi	Compressive strength of concrete (ksi)
J _c 4.000 kSt	compressive strength of concrete (ksr)
$f_y \coloneqq 60 \ ksi$	Yield strength of concrete reinforcing steel (ksi)
$H_r \coloneqq 43.0 \ in$	Total height of bridge rail system measured from the top of the roadway surface/overlay to the top of highest rail (in.)
$H_R := 24.00 \ in$	Height of the bridge rail system measured from the top of the roadway surface/overlay to the centroid of the steel rail elements (in.)
$curb_{ht} = 6$ in	"Height of curb (inches)"
$t_0 := 0.0 \ in$	Thickness of overlay (in.)

(1b) Concrete deck and curb inputs:

$H_{curb} \coloneqq 6.0 \ in$	Height of Curb (in.)
$t_{deck} \! \coloneqq \! 8.0 \; \textit{in}$	Thickness of Deck (inches)

(1b) Steel Rail, Post, and Anchor Rod Inputs:

Steel Rail Inputs:	
a) Use 10 gage Thrie Beam (50 ksi) b) Use W6x15 Posts Fy = 50 ksi	
$F_{yR} = 50 \ ksi$ Yield strength of steel rail (ksi)	
$h_R\!\coloneqq\!20in$ Height of a single steel rail (in)	
$N_R\!\coloneqq\!1$ Number of steel rail elements	
$Z_R := 47000 \ mm^3 \cdot 1.15 = 3.298 \ in^3$	Plastice Section Modulus of Rail (in^3)



a) Steel Post is W6x	15
D) A992 I y = 50 Ksi	
$F_{yP} \coloneqq 50 \ \kappa si$	Yield strength of steel post (ksi)
$w_p \coloneqq 6 \ in$	Width of steel post about the bending axis (in.)
$t_w \coloneqq 0.23$ in	Thickness of steel post web (in.)
$t_f := 0.26 \ in$	Thickness of flange (in)
$Z_P := 10.8 \ in^3$	Plastice Section Modulus of Post (in^3)
$L_p := 3 \; ft + 1.5 \; in$	Steel post spacing (ft)
chor Rod Inputs:	
a) Anchor Rods are I	Hilti HAS-E Rods, Fu = 120 ksi
a) Anchor Rods are l b) Anchor Rods are f $F_{u.rod} \coloneqq 120~ksi$	Hilti HAS-E Rods, Fu = 120 ksi 7/8" ∲ x 10" embedded 7 inches Tensile strength of anchor rods (ksi)
a) Anchor Rods are l b) Anchor Rods are ' $F_{u.rod} \coloneqq 120 \ ksi$ $N_{rod} \coloneqq 4$	Hilti HAS-E Rods, Fu = 120 ksi 7/8" \$\u03e8 x 10" embedded 7 inches Tensile strength of anchor rods (ksi)
a) Anchor Rods are i b) Anchor Rods are i $F_{u.rod} \coloneqq 120$ ksi $N_{rod} \coloneqq 4$ $N_{rod.tension} \coloneqq 2$	Hitti HAS-E Rods, Fu = 120 ksi 7/8" \u03c6 x 10" embedded 7 inches Tensile strength of anchor rods (ksi) Number of anchor rods Number of anchor rods in tension
a) Anchor Rods are 1 b) Anchor Rods are $P_{u.rod} = 120$ ksi $N_{rod} = 4$ $N_{rod.tension} = 2$ $d_{rod} = 10$ in	Hitti HAS-E Rods, Fu = 120 ksi 7/8" \u0395 x 10" embedded 7 inches Tensile strength of anchor rods (ksi) Number of anchor rods Number of anchor rods in tension
a) Anchor Rods are i b) Anchor Rods are i $F_{u.rod} \coloneqq 120 \ ksi$ $N_{rod} \coloneqq 4$ $N_{rod.tension} \coloneqq 2$ $d_{rod} \coloneqq 10 \ in$ $\phi_{rod} \coloneqq \frac{7}{8} \ in$	Hilti HAS-E Rods, Fu = 120 ksi 7/8" \u03c6 x 10" embedded 7 inches Tensile strength of anchor rods (ksi) Number of anchor rods Number of anchor rods in tension Distance from the anchor rods acting in tension to the back of the steel plate (in.)
a) Anchor Rods are 1 b) Anchor Rods are 1 $F_{u.rod} \coloneqq 120 \ ksi$ $N_{rod} \coloneqq 4$ $N_{rod.tension} \coloneqq 2$ $d_{rod} \coloneqq 10 \ in$ $\phi_{rod} \coloneqq \frac{7}{8} \ in$	Hilti HAS-E Rods, Fu = 120 ksi 7/8" \$\u03e8 x 10" embedded 7 inches Tensile strength of anchor rods (ksi) Number of anchor rods Number of anchor rods in tension Distance from the anchor rods acting in tension to the back of the steel plate (in.) Diameter of anchor rods (in.)
a) Anchor Rods are 1 b) Anchor Rods are 1 $F_{u.rod} := 120 \ ksi$ $N_{rod} := 4$ $N_{rod.tension} := 2$ $d_{rod} := 10 \ in$ $\phi_{rod} := \frac{7}{8} \ in$	Hilti HAS-E Rods, Fu = 120 ksi 7/8" \phy x 10" embedded 7 inches Tensile strength of anchor rods (ksi) Number of anchor rods Number of anchor rods in tension Distance from the anchor rods acting in tension to the back of the steel plate (in.)
a) Anchor Rods are 1 b) Anchor Rods are 1 $F_{u.rod} \coloneqq 120 \ ksi$ $N_{rod} \coloneqq 4$ $N_{rod.tension} \coloneqq 2$ $d_{rod} \coloneqq 10 \ in$ $\phi_{rod} \coloneqq \frac{7}{8} \ in$	Hilti HAS-E Rods, Fu = 120 ksi 7/8" \$ x 10" embedded 7 inches Tensile strength of anchor rods (ksi) Number of anchor rods Number of anchor rods in tension Distance from the anchor rods acting in tension to the back of the steel plate (in.) Diameter of anchor rods (in.)
a) Anchor Rods are 1 b) Anchor Rods are 1 $F_{u.rod} \coloneqq 120 \ ksi$ $N_{rod} \coloneqq 4$ $N_{rod.tension} \coloneqq 2$ $d_{rod} \coloneqq 10 \ in$ $\phi_{rod} \coloneqq \frac{7}{8} \ in$	Hilti HAS-E Rods, Fu = 120 ksi 7/8" \$ x 10" embedded 7 inches Tensile strength of anchor rods (ksi) Number of anchor rods Number of anchor rods in tension Distance from the anchor rods acting in tension to the back of the steel plate (in.) Diameter of anchor rods (in.)
a) Anchor Rods are i b) Anchor Rods are i $F_{u.rod} \coloneqq 120 \ ksi$ $N_{rod} \coloneqq 4$ $N_{rod.tension} \coloneqq 2$ $d_{rod} \coloneqq 10 \ in$ $\phi_{rod} \coloneqq \frac{7}{8} \ in$	Hilti HAS-E Rods, Fu = 120 ksi 7/8" \phy x 10" embedded 7 inches
a) Anchor Rods are i b) Anchor Rods are i $F_{u.rod} \coloneqq 120 \ ksi$ $N_{rod} \coloneqq 4$ $N_{rod.tension} \coloneqq 2$ $d_{rod} \coloneqq 10 \ in$ $\phi_{rod} \coloneqq \frac{7}{8} \ in$	Hilti HAS-E Rods, Fu = 120 ksi 7/8" \$ x 10" embedded 7 inches Tensile strength of anchor rods (ksi) Number of anchor rods Number of anchor rods in tension Distance from the anchor rods acting in tension to the back of the steel plate (in.)



		esign For	ces for Tra	mic Railin	igs:			
Test Level	Rail Height (in.)	F _t (kip)	F _L (kip)	F _v (kip)	L _t /L _L (ft)	L _v (ft)	H _e (in)	H _{min} (in)
TL-1	18 or above	13.5	4.5	4.5	4.0	18.0	18.0	18.0
TL-2	18 or above	27.0	9.0	4.5	4.0	18.0	20.0	18.0
TL-3	29 or above	71.0	18.0	4.5	4.0	18.0	19.0	29.0
TL-4 (a)	36	68.0	22.0	38.0	4.0	18.0	25.0	36.0
TL-4 (b)	between 36 and 42	80.0	27.0	22.0	5.0	18.0	30.0	36.0
TL-5 (a)	42	160.0	41.0	80.0	10.0	40.0	35.0	42.0
TL-5 (b)	greater than 42	262.0	75.0	160.0	10.0	40.0	43.0	42.0
TL 6		175.0	58.0	80.0	8.0	40.0	56.0	90.0
$TL \coloneqq 4$	Test level							
NCI	HRP Project 22-20(2)		0				
TT 4	Testinus							
114	lestiever							
$F_t := 80$	<i>kip</i> Transve	rse impact fo	rce (kips)					
$L_t \coloneqq 5.0$	ft Longitud	dinal length o	f distribution o	f impact force	e (ft)			
$H_e \coloneqq 30$	<i>in</i> Height d	of equivalent f	ransverse loa	d from top of	overlay (in.)			
$H_{min} := 3$	36.0 <i>in</i> Minimur	n height of a	MASH TL-3 b	arrier (in.)				
$h_e \coloneqq H_e$	$+t_0 = 30 in$	Total equ	iivalent transv	erse impact h	neight (in.)			
$H_r = 43$	in	Total height o surface/overl	of bridge rail s ay to the top o	ystem measu of highest rail	red from the to (in.)	p of the road	lway	







$_{post} = 6 \ in \qquad H_r$	=43 <i>in</i>			
EA = 26 in				
$ratio_{\Sigma AH} \coloneqq \frac{\Sigma A}{H_r} = 0.6$	05			
$Set_{low.x} \coloneqq \begin{bmatrix} 0 & 1 & 2 & 3 & 4 \end{bmatrix}$	$5\ 6\ 7\ 8\ 9\ 10]$			Lower boundary for post setback criteria x and y
$Set_{low.y} := [0.75 \ 0.63 \ 0]$	0.52 0.4 0.315 0.28	0.27 0.26 0.	$25 \ 0.245 \ 0.245]$	coordinates
$Set_{up,x} := [2.5 \ 3 \ 4 \ 5 \ 6]$	378910]		· · · · · · · · · · · · · · · · · · ·	Upper boundary for post setback criteria x and y coordinates
$Set_{up.y} := [0.8 \ 0.725 \ 0.5]$.6 0.5 0.46 0.44 0.4	$43_{-}0.425_{-}0.42$	2]	
$Set_{sys.x} \coloneqq \frac{s_{post}}{in} = 6$			Post setback rail ge	eometric point
$Set_{sys.x} \coloneqq rac{s_{post}}{in} = 6$ $Set_{sys.y} \coloneqq ratio_{\SigmaAH} = 0.6$	605		Post setback rail g	eometric point dth to total height rail geometric poi
$Set_{sys.x} := \frac{s_{post}}{in} = 6$ $Set_{sys.y} := ratio_{\SigmaAH} = 0.6$	605 Set _{tor.d} Set _{tor.j}	Set _{up.2} Se	Post setback rail go Ratio of contact wire	cometric point
$Set_{sys,x} := \frac{s_{post}}{in} = 6$ $Set_{sys,y} := ratio_{\SigmaAH} = 0.6$	605 Set _{ion.} , Set _{ion.}	Set _{up.} Se	Post setback rail gr	sometric point
$Set_{sys.x} \coloneqq \frac{s_{post}}{in} = 6$ $Set_{sys.y} \coloneqq ratio_{\SigmaAH} = 0.6$	605 Set _{ton.2} Set _{ton.3} 0 0.75 1 0.63	Set _{up.} Se	Post setback rail gr	sometric point
$Set_{sys.x} \coloneqq \frac{s_{post}}{in} = 6$ $Set_{sys.y} \coloneqq ratio_{\SigmaAH} = 0.6$		Set _{up.} Se 	Post setback rail gr Ratio of contact wire twp.p	cometric point
$Set_{sys.x} := \frac{s_{post}}{in} = 6$ $Set_{sys.y} := ratio_{\Sigma AH} = 0.6$	505 $(Set_{ton,y})$ $(Set_{ton,y})$ 0 0.75 1 0.63 2 0.52 3 0.4	Set _{up.} , Se 2.5 0 3 0. 4 0 5 0	Post setback rail gr Ratio of contact wire tupy	cometric point
$Set_{sys.x} := \frac{s_{post}}{in} = 6$ $Set_{sys.y} := ratio_{\SigmaAII} = 0.6$	605 Set _{ion.2} Set _{ion.3} 0 0.75 1 0.63 2 0.52 3 0.4 4 0.315	$\begin{array}{c c} Set_{np2} & Set\\ \hline 2.5 & 0\\ \hline 3 & 0.'\\ 4 & 0\\ 5 & 0\\ \hline 6 & 0. \end{array}$	Post setback rail ge Ratio of contact wie kupp 8.8 725 9.6 9.5 46	sometric point
$Set_{sys,x} := \frac{s_{post}}{in} = 6$ $Set_{sys,y} := ratio_{\SigmaAH} = 0.6$	$\begin{array}{c} 605 \\ \hline \\ 0 \\ 0$	$\begin{array}{c c} Set_{up,r} & Se\\ \hline \\ \hline$	Post setback rail gr Ratio of contact wire twp.p 1.8 725 1.6 1.5 46 44	sometric point
$Set_{sys.x} := \frac{s_{post}}{in} = 6$ $Set_{sys.y} := ratio_{\Sigma AH} = 0.6$	$\begin{array}{c c} \hline & \\ \hline \hline & \\ \hline \\ \hline$	Set _{up.s} Se 2.5 C 3 0. 4 C 5 C 6 0. 7 0. 8 0.	Post setback rail gr Ratio of contact wire tupp)	sometric point
$Set_{sys.x} := \frac{s_{post}}{in} = 6$ $Set_{sys.y} := ratio_{\SigmaAH} = 0.6$	Setton.s Setton.s 0 0.75 1 0.63 2 0.52 3 0.4 4 0.315 5 0.28 6 0.27 7 0.26	Set _{up.s} Se 2.5 0 3 0. 4 0 5 0 6 0, 7 0, 8 0. 9 0.	Post setback rail gr Ratio of contact with twp	sometric point
$Set_{sys.x} := \frac{s_{post}}{in} = 6$ $Set_{sys.y} := ratio_{\Sigma A H} = 0.6$	Setion: Setion: 0 0.75 1 0.63 2 0.52 3 0.4 4 0.315 5 0.28 6 0.27 7 0.26 8 0.25	$Set_{102.7}$ Set 2.5 00 3 0. 4 00 5 00 6 0. 7 0. 8 0. 9 0. 10 0.	Post setback rail gr Ratio of contact wire tung 8 8 725 8 8 725 8 8 725 8 8 725 8 8 725 7 8 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	eometric point
$Set_{sys.x} \coloneqq \frac{s_{post}}{in} = 6$ $Set_{sys.y} \coloneqq ratio_{\Sigma A II} = 0.6$	Section:: Section:: 0 0.75 1 0.63 2 0.52 3 0.4 4 0.315 5 0.28 6 0.27 7 0.26 8 0.25 9 0.245	$\begin{array}{c c} Set_{up,r} & Set\\ \hline 2.5 & 0\\ \hline 3 & 0.'\\ 4 & 0\\ 5 & 0\\ \hline 6 & 0.\\ 7 & 0.\\ 8 & 0.\\ 9 & 0.\\ 10 & 0.\\ \end{array}$	Post setback rail gr Ratio of contact wire twpp 8.8 725 	sometric point
$Set_{sys.x} := \frac{s_{post}}{in} = 6$ $Set_{sys.y} := ratio_{\SigmaAII} = 0.6$	Section:: Section:: 0 0.75 1 0.63 2 0.52 3 0.4 4 0.315 5 0.28 6 0.27 7 0.26 8 0.25 9 0.245	$Set_{up.r}$ Set 2.5 0 3 0.4 4 0 5 0 6 0. 7 0. 8 0. 9 0.4 10 0.	Post setback rail gr Ratio of contact wire tupped 18 18 18 19 19 19 10 10 10 10 10 10 10 10 10 10 10 10 10	sometric point
$Set_{sys.x} \coloneqq \frac{s_{post}}{in} = 6$ $Set_{sys.y} \coloneqq ratio_{\Sigma AH} = 0.6$	Settor. Settor. 0 0.75 1 0.63 2 0.52 3 0.4 4 0.315 5 0.28 6 0.27 7 0.26 8 0.25 9 0.245 10 0.245	Setup. Set 2.5 0 3 0.' 4 0 5 0 6 0, 7 0, 8 0, 9 0, 10 0,	Post setback rail gr Ratio of contact with tup	sometric point





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Ì	Ch	eck	Pc	st_{st}	Set	bac	k_C	rit	erie	a :=	if	Po	st_S	betbe	ack_{-}	Cri	iter	ria_	Rai	l_{c}	Geo	met	ric	P	oin	$t \ge$	2		
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4) Steel Rail & F	Post Strength Analysis:
$F_{yR} = 50 \ ksi$	Yield Strength of all steel rail elementsl (ksi)
$Z_R = 3.298 \ in^3$ $n_R := 1$	Plastic Sectional Modulus of the Steel Thrie Beam (in.3) Number of Tube Rail
$H_{thrie} \coloneqq 34.75$	$in - \left(\frac{300 \ mm}{2}\right) = 24.789 \ in$
$M_{pthrie} \coloneqq n_R \cdot F_{yR} \cdot 2$	$Z_R\!=\!13.743\; m{kip}\!\cdot\!m{ft}$ Plastic Moment Capacity of the Steel Tube Rail (kip-ft)
Z _{HSS} := 19.0 <i>in</i>	$H_{HSS} := 41 \text{ in } HSS10x4x1/4 \text{ Top Tube}$
$M_{pHSS} \coloneqq Z_{HSS}$	$F_{yR} = 79.167 \ kip \cdot ft$
$M_p \coloneqq M_{pHSS} + $	$M_{pthrie} = 92.91 \ kip \cdot ft$
$\boldsymbol{Y_{rails}} \coloneqq \frac{M_{pthrie}}{M_{rails}}$	$\frac{\cdot H_{thrie} + M_{pHSS} \cdot H_{HSS}}{M_p} = 38.602 \ in$
$h_p \coloneqq Y_{rails} - curbon $	Height from the bottom of the post to the centroid of the steel rail (in.)
$h_p = 32.602$ in	
$H_p\!\coloneqq\!h_p\!+\!curb$	$h_{tt} = 38.602 \ in$
Calculate the Plas	tic Strength of the Post: P_{P1}
$Z_P\!=\!10.8\;{in}^3$ Ben	stic Sectional Modulus of the Steel Post about the ding axis (in.)
$F_{yP} = 50 \ ksi$	Yield strength of steel post (ksi)
$\mathcal{M}_{post} \coloneqq F_{yP} \bullet Z_P = 4$	5 $kip \cdot ft$ Plastic strength of the Steel Post (kip-ft)
$n_p = 32.602 \ in$	Height from the bottom of the post to the centroid of the rail elements (in.)
$P_{P1} := \frac{M_{post}}{h} = 16.56$	63 <i>kip</i> Post strength based on the plastic failure of a steel post @

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$F_{u,rod} = 120 \ ks$	i Tensile strength of the anchor rod	s (ksi)
$\phi_{rod} = 0.875$ in	Diameter of anchor (in.)	
$\mathbf{A}_{rod} \coloneqq \frac{\pi}{4} \cdot \phi_{rod}$	${n_i}^2=0.601~{m in}^2$ Area of a single a	nchor rod (in.)
$R_{nt} \coloneqq F_{u.rod} \cdot (0)$	$(0.75 \cdot A_{rod}) = 54.119 \; kip$ Nomi	nal strength of one anchor rod in tension (kip)
$V_{rod.tension} = 2$	Number of anchor rods acting in tension	on
$d_{rod} = 10$ in	Distance from the anchor rods acting i back of the steel plate (in.)	in tension to the
$l_b := 1.5 \ in$	Length of the steel plate bearing press concrete parapet (in.)	sure acting on the
$w_{rod} \coloneqq d_{rod}$	$-\frac{a_b}{3}=9.5 \ in$	Distance from anchor rods acting in tension to the centroid of the bearing pressure acting on the concrete parapet (in.)
$M_{t.rod} \coloneqq w_{rot}$	$_{od} \cdot R_{nt} \cdot N_{rod.tension} = 85.688 \ kip$	• ft Moment strength of post based on tensile capacity of anchor rods (kip-ft)
$h_p = 32.602$	in	Height from the bottom of the post to the centroid of the steel tube (in.)
$P_{t.rod} \coloneqq \frac{M_t}{h}$	$\frac{1}{p} = 31.54 \ kip$	Post strength based on the tensile capacity of anchor rods (kip)
$R_{nv} \coloneqq F_{u.roo}$	$_{i} \cdot (0.45 \cdot A_{rod}) = 32.471 \ kip$	Nominal strength of one anchor rod in shear w/ treads in shear plane (kip)
$P_{v.rod} \coloneqq N_{rot}$	_{bd} •R _{nv} =129.885 <i>kip</i>	Post strength base on the shear capacity of anchor rods (kip)
P_{P2} :=min	$(P_{t,rod}, P_{v,rod}) = 31.54 \ kip$	Post strength base on the ultimate strength of the anchor rods (kip)

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P_{P_4}										
	Use Hilti inches n	RE500 V nin.	3 Epoxy fo	or 3/4" DI.	A. Anch	ors Embec	lded 7			
Reference:	Table 25	- Hilti RE	-500 V3 E	poxy Adh	esive D	esign Strei	ngth w	ith		
concrete bo	ond failur	e for threa	ided rod ir	uncrack	ed Conc	rete, 2016	Desig	n Gui	ide,	
page 151										
			45000	= 7" depti	n					
$F_{T_\phi N} \coloneqq$	45000 <i>lb</i>	f	Extrapolat inches fro	ed ultima m TTI Tes	te Stren sting of a	gth for em anchor with	beddeo n RE50	d dep 0V3	th = 7	
From Ta	ble 38 - L	oad Adju	stment fac	tors for 7	/8" Diam	neter threa	ded ro	ds in		
uncrack	ed concre	ete, Hilti D	esign Gui	de, page	158					$h_p = 32.602$
f_A	$_{\rm N} := 0.71$		Spacing F	actor in te	ension (*	11	fume	=0.9	140	dea.
J 71	N		inches and	chor spac	ing)		5 temp		temp).
									redu	ction
f_{μ}	$_{\rm M} = 0.49$		Edae D	istance re	eduction	factor for				
5 11	2 4		tension	(5 inches	s edge c	listance)		0.	4 = 7'	' depth
F_{TRE500} :	$=F_{T_{-}\phi N}$ •	$f_{AN} \cdot f_{RN} \cdot$	$f_{temp} \cdot 1.5$	=21.135	kip	Edge di values f	stance rom Hi	and s Iti are	spacir	ıg
	F	10 / 0				conserv	ative fo	or reir	nforce	d
$P_{PA} =$	$=\frac{F_{TRE500}}{T_{TRE500}}$	• 10 <i>in</i> • 2	= 12.965	kip		concrete	e use 1	.5 fac	ctor fo	r
11		h_p		-		loading	ed and	dyna	mic	
Iculate the V	Veld Stre	ngth of Po	<u>st Joint:</u>	P_{P4}			(.4•6)+{1	.0.1)	0.420
							<u> </u>	7	,	-=0.486
eld.joint := 0.0	un -	vviath of wei	aea joint (in.)							
$_{eld.joint} \coloneqq 6.0$) <i>in</i>	Depth of wel	ded joint (in.)							
$_{cld.joint} := 0.7$	$07 \cdot 0.25$	<i>in</i> Thic	kness of weld	ing (in.)						
)() Strengt	h reduction fa	ictor for welde	ed ioint						
ea.yom				,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	Section r	nodulus about	hrizontal	axis x-	x (in 2)	
		7	2		Wel	d Treated a	s a line	for a	ŵ-	
$:= 2 \cdot b_{weld.jo}$	$_{int}$ • d_{weld}	$_{joint} + \frac{d_{we}}{d_{we}}$	$\frac{ld.joint}{3} = 8$	84 <i>in</i> ²	Sha bas	pe welded a	all arou	nd on	а	
$70XX \coloneqq 70$	k <i>si</i> Ele	ctrodes (ksi)								
Ø	$\cdot S_w \cdot t_{wold}$	$_{ioint} \cdot E702$	XX							
	. w wc40	.j. 00100	0107	0.1.1.	1 1 1 1 1	In the basis				

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$P_{P1} = 16.563 \ kip$	Post strength based on the	e plastic failure of a steel post (kip)
P _{P2} =31.54 <i>kip</i>	Post strength base on the rods (kip)	eultimate strength of the anchor
$P_{P3} = 19.261 \ kip$	Post strength based on the resistance of concrete from	ie vertical punching shear m traffic side anchor rods (kip)
$P_{P4} = 12.965 \ kip$	Post Strength based on ac anchors (kip) 7" anchor	dhesive bond strength of r embedment
$P_{P5}\!=\!31.878\; {m kip}$	Post strength based of Welds (kips)	on strength
$P_P \coloneqq min\left(P_{P1}, P_{P2}, \ldots\right)$	$(P_{P3}, P_{P4}, P_{P5}) = 12.965 \ ki$	ip Post strength found by using the limiting ("Worst case") post strength (kips)
	$P_P = 12.965 \ {\it kip}$ o	imiting Post Strength Based on Bond Failure close to
	p	











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